



# Analysis and Design of Left-Handed Metamaterial Lenses Using Ansoft HFSS



Anthony Lai<sup>1</sup>, Kevin M.K.H. Leong<sup>1</sup>, Christophe Caloz<sup>2</sup>,  
and Tatsuo Itoh<sup>1</sup>

<sup>1</sup>University of California, Los Angeles, 405 Hilgard Ave., Los Angeles, CA 90095, USA

<sup>2</sup>École Polytechnique, Montréal, 3333 Queen Mary, H3V1A2, QC, Canada



The banner for the CONVERGE 2005 Applications Workshop features a large, stylized 'C' containing the word 'CONVERGE'. Below it, the text 'AN APPLICATIONS WORKSHOP FOR HIGH-PERFORMANCE DESIGN' is visible. The banner is divided into three main sections: 'RFIC, MMIC, ANTENNA, RADIO' on the left, 'SIGNAL INTEGRITY, HIGH-SPEED SERIAL, PACKAGING, SSO, EMI/EMC' in the center, and 'AUTOMOTIVE, DEFENSE, VHDL-AMS AEROSPACE, AND POWER' on the right. At the bottom, there is a call to action: 'Register today for Ansoft's 2005 Worldwide Applications Workshop, Converge. Meet industry experts and learn new design methodologies for High Performance IC, Microwave, Signal Integrity, and Electromechanical Design.'

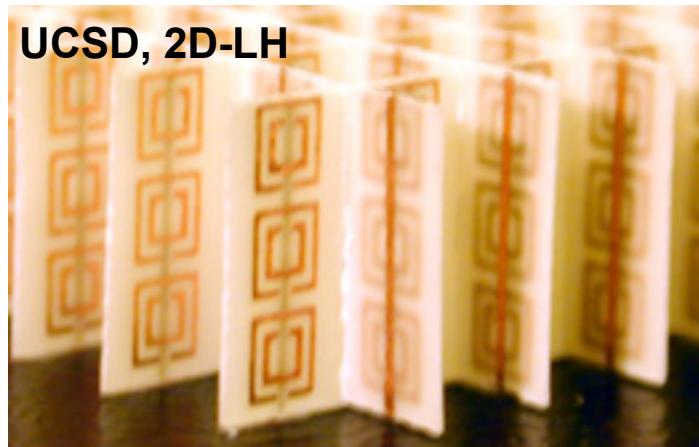


### Historical Milestones

- 1968 : theoretical analysis of hypothetical LH materials by Veselago
- 1996/9 : introduction of electric ( $\epsilon < 0$ ) / magnetic ( $\mu < 0$ ) plasmon by Pendry
- 2000 : experimental demonstration of LH structure by Smith

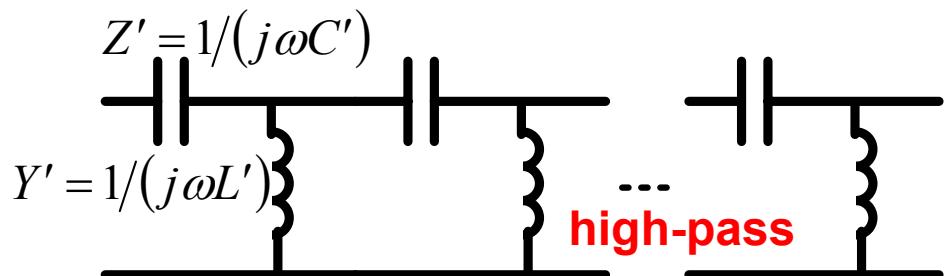
LH definition: → materials with  $\epsilon < 0$  and  $\mu < 0 \Rightarrow n < 0$  and  $v_p - \| v_g$   
 → unit-cell  $\ll \lambda$  → **effective / macroscopic / homogeneous**

### Resonant Structure Approach



- approach: no simple/rigorous analysis & no design method
- structures: **RESONANT** ⇒ **lossy & narrow bandwidth** & **highly dispersive**

### Transmission Line Approach

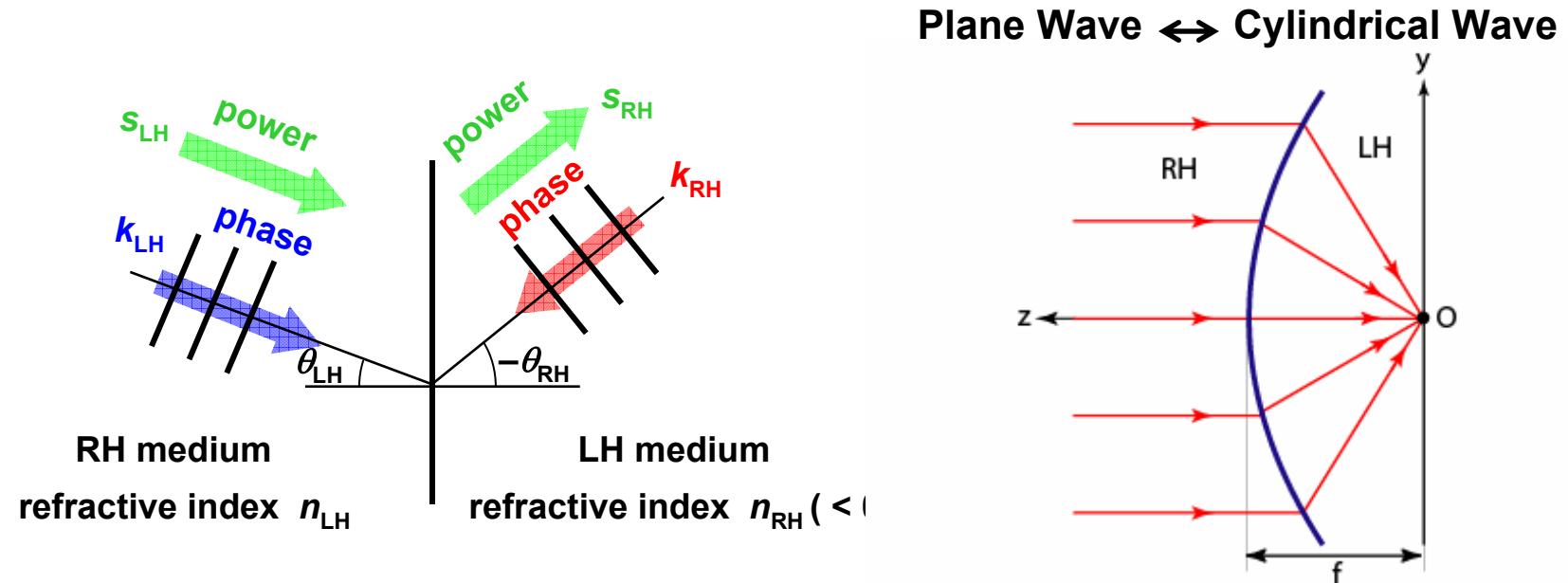


**“BACKWARD WAVES”**

(e.g. Brillouin, Pierce)

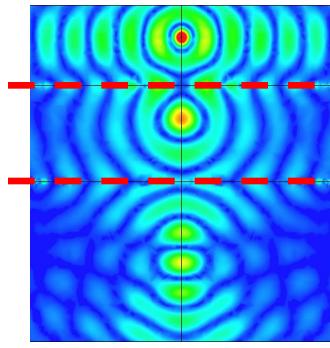
- approach: Transmission line analysis & circuit design methods
- structures: **NON-RESONANT** ⇒ **low loss & broad bandwidth** & **moderate dispersion**

# Negative Refractive Index Lenses

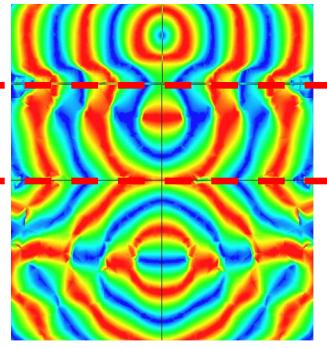


## HFSS Simulations: Effective Medium ( $\epsilon < 0, \mu < 0$ )

flat lens

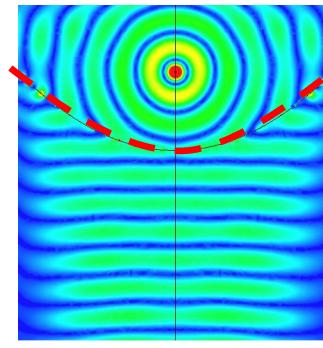


magnitude

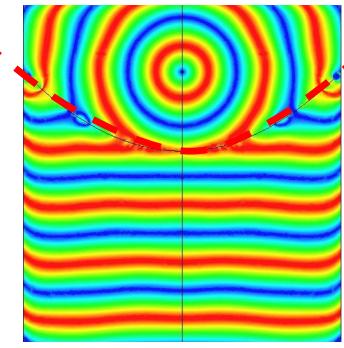


phase

parabolic lens

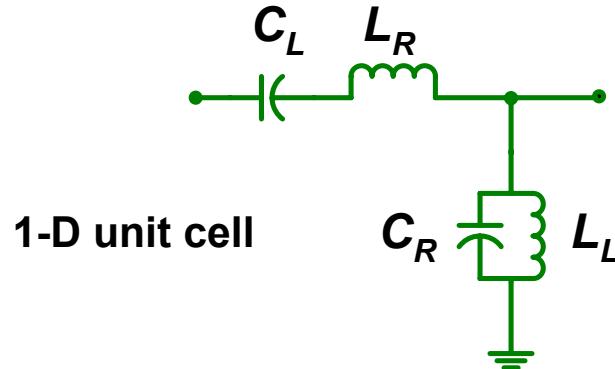


magnitude

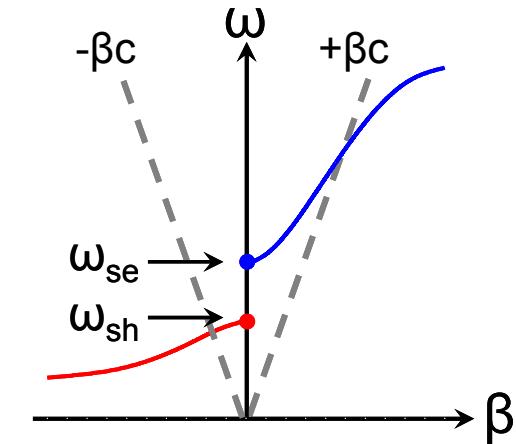


phase

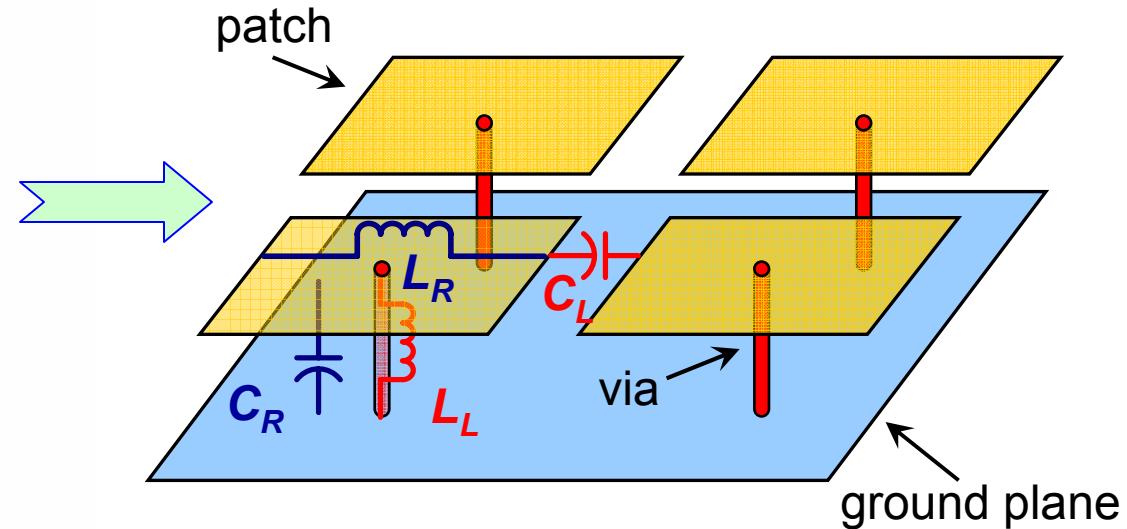
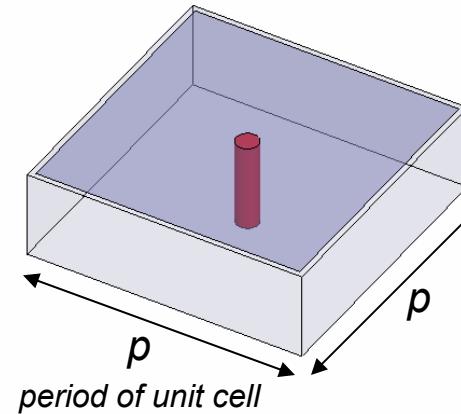
### Composite Right/Left-Handed TL



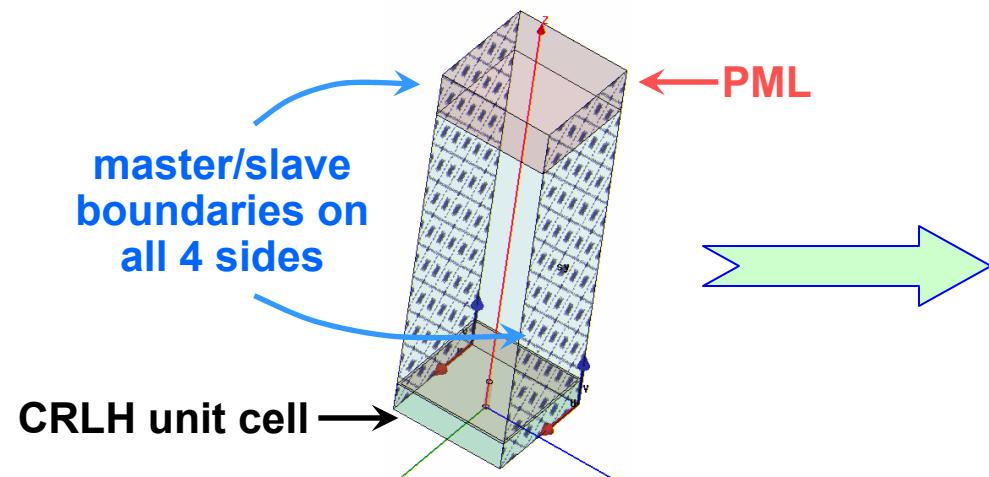
CRLH metamaterial includes  
LH and unavoidable  
RH parasitic effects.  
**LH at low frequencies**  
**RH at high frequencies**



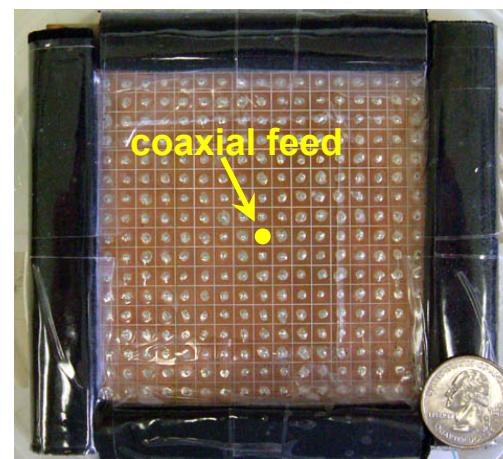
### 2-D unit cell



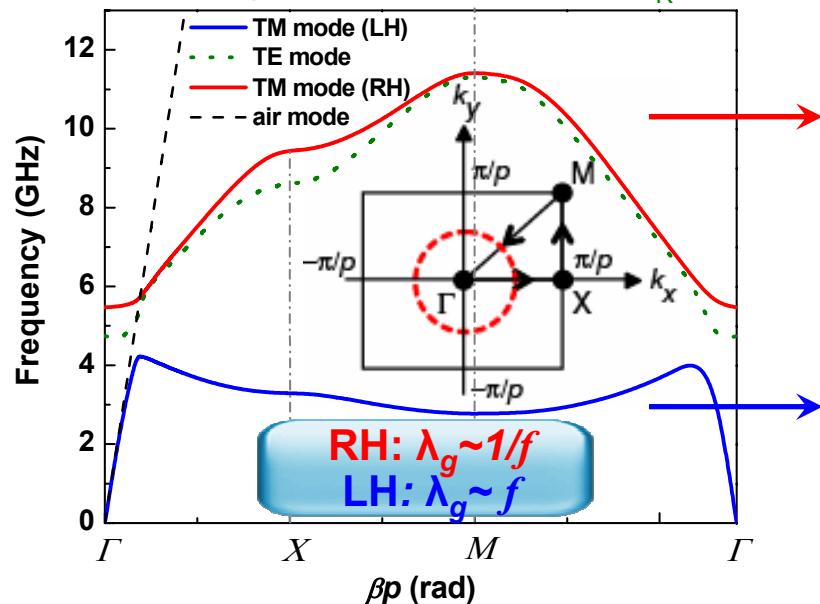
## HFSS Eigenmode Simulation w/PBCs



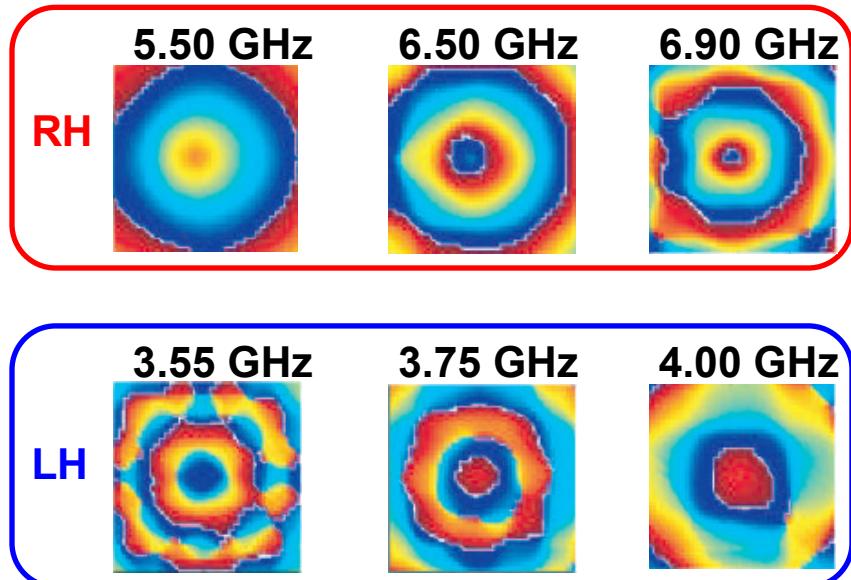
## 17x17 Mushroom Array



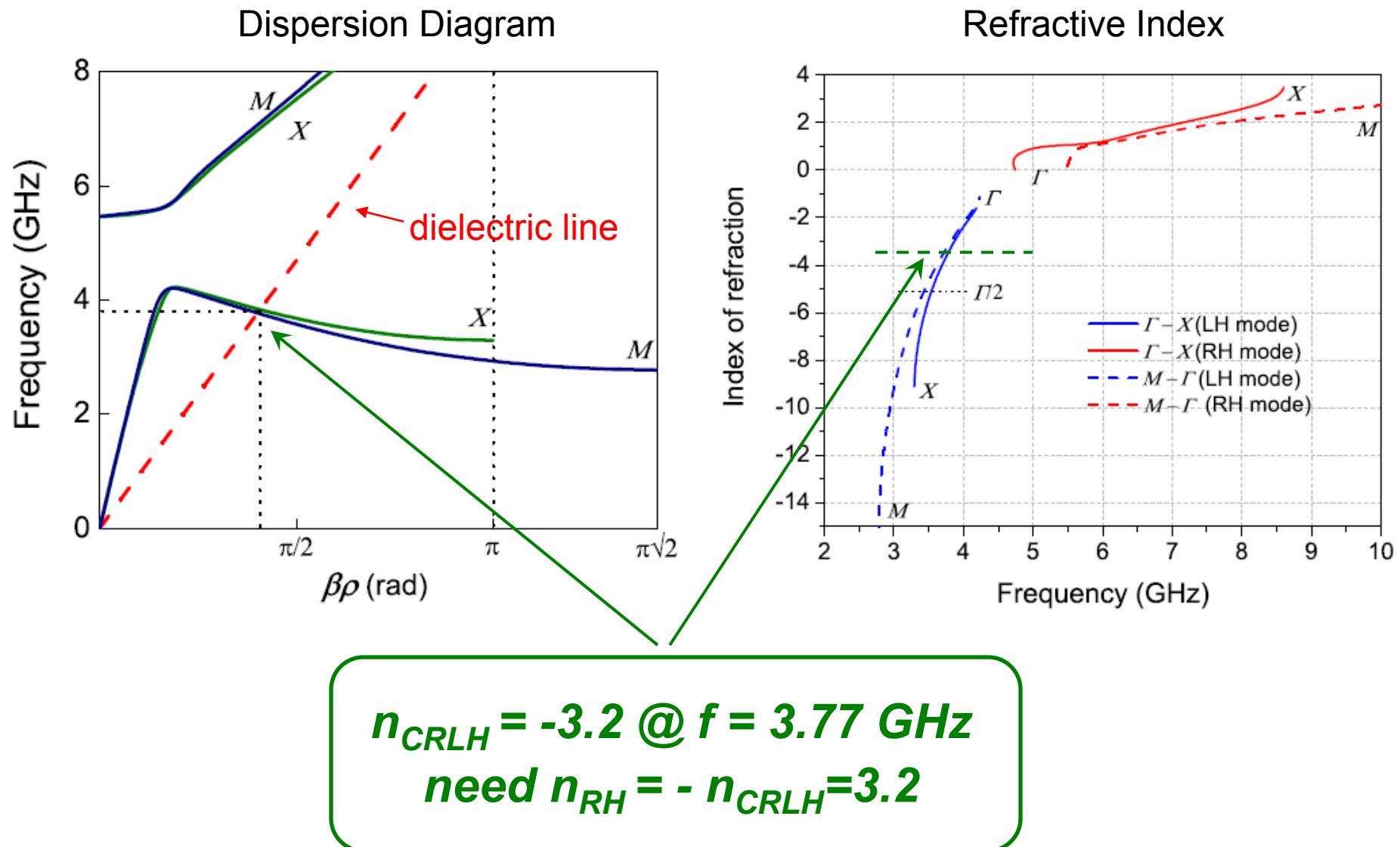
**Dispersion Diagram (HFSS)**  
( $p=5.0$  mm,  $g=1.0$  mm,  $h=1.27$  mm,  $\epsilon_R=10.2$ )

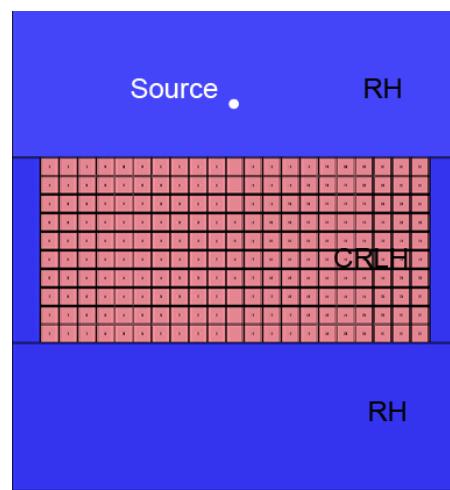


## Measured E-Field Phase Atop 17x17 Array

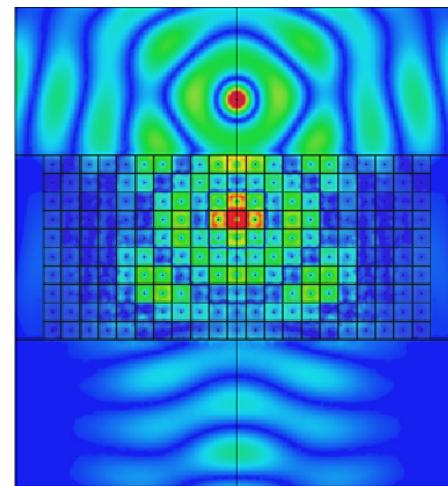


# RH/LH Interface Matching Conditions

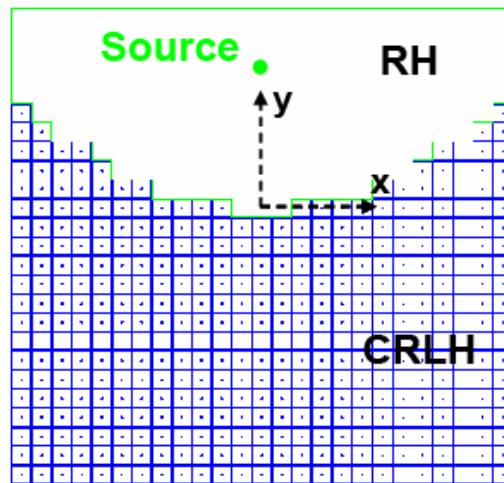
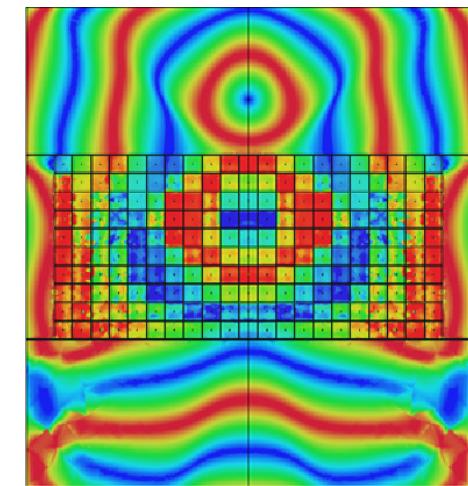




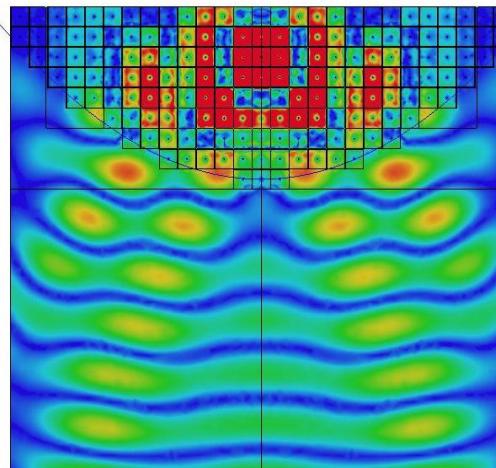
magnitude



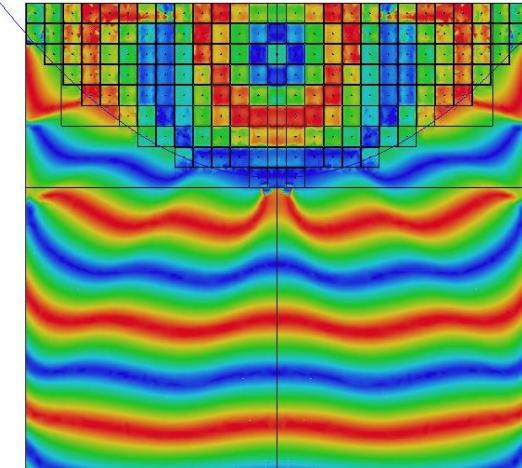
phase



magnitude

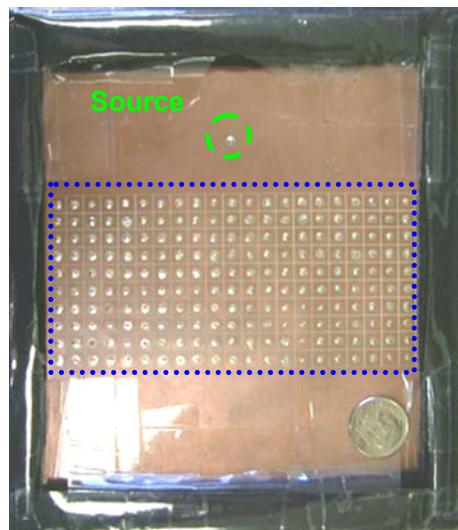


phase

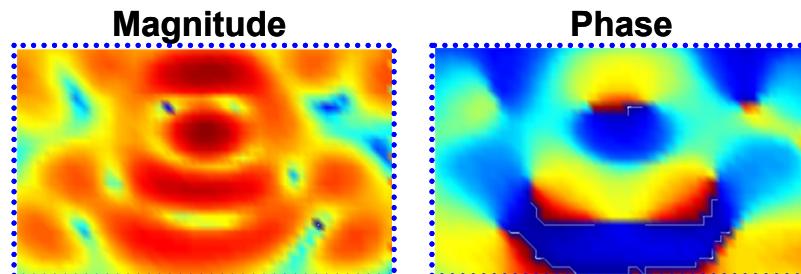


\* CRLH and RH regions interchanged for simulation

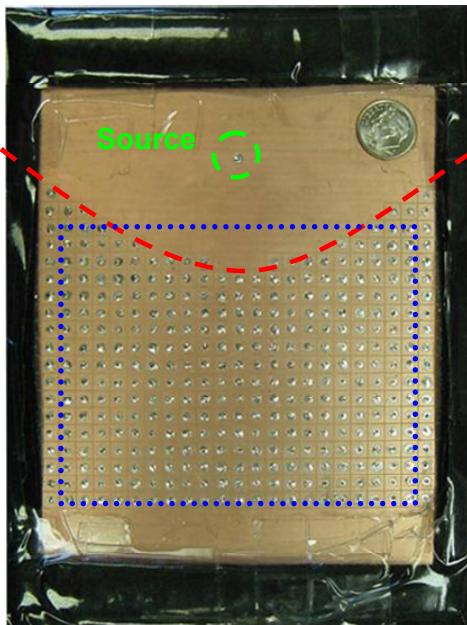
# Measured Results



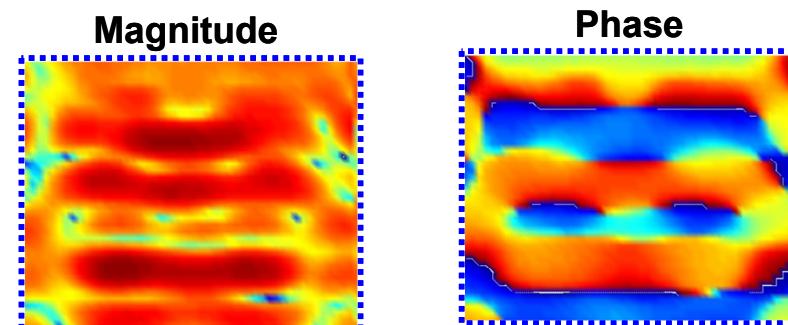
$$f_0 = 3.79 \text{ GHz}$$



Mushrooms (21x10 cells)  
\* Entire structure built on  $\epsilon_R = 10.2$  substrate



$$f_0 = 3.77 \text{ GHz}$$



~ Mushrooms (23x16 cells) in  
outlined area